

- A. AIAT and converse
- B. \times sums.
- C. From Δ s to polygons

Mon 8/28: I. Questions or HW

- II. Show coral picture as an example of hyperbolic geometry in nature.
- III. Intro to Tex.

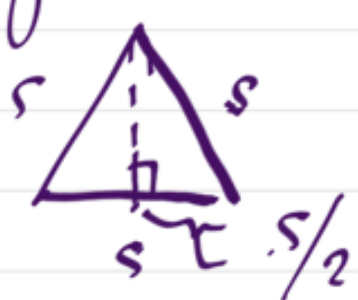
Wed. 8/30: I. Tiling the plane

A. what shapes are possible & why?

B. How does perimeter of a cell translate into total perimeter?

Sol. let $N = \#$ of cells. The $P_T \approx N \cdot p$, that is, give P_T , what shape will yield the largest area? Of course, $A_T = NA$, so we simply want find largest ratio A/p .

II, let's work out the ratio
for an equilateral Δ :


$$\left. \begin{array}{l} \text{Diagram of an equilateral triangle with side length } s. \\ \text{The height } h \text{ is shown as a dashed line from the top vertex to the base.} \\ \text{The base is divided into two segments of length } s/2. \end{array} \right\} h = \sqrt{s^2 - \left(\frac{s}{2}\right)^2} = \sqrt{\frac{3}{4}s^2} = \frac{s\sqrt{3}}{2}.$$

$$\text{So } A = \frac{1}{2}sh = \frac{1}{2}s \left(\frac{s\sqrt{3}}{2}\right) = \frac{s^2\sqrt{3}}{4}.$$

$$P = 3s, \text{ so } A/P = \frac{s^2\sqrt{3}/4}{3s} = s \frac{\sqrt{3}}{12}.$$

Hum! Better to use $S = \frac{P}{3}$;
hence $\frac{A}{P} = P \frac{\sqrt{3}}{36}$.

Although the ratio does depend
on P — is there a general principle
here? Why are animals that live
in colder places larger? — This
won't matter, because P will be held
constant.

(So what determines P for the bees?
Probably, the area of the cells.)

We have what we need, but for additional interest and practice:

$$A = \frac{P^2 \sqrt{3}}{36}, \text{ so } P = \dots$$

III. The square is easy. What about the hexagon? Don't just look up a formula!! Work it out for yourself. What are some ways you could do that?

Fri 9/1 I. Hand out Ch. 2.

II. A. How did students learn about area? Develop basic properties of invariance + additivity. Can proceed from unit or from continuous definition.

B. Develop area of other figures:
Have students explain the formulas!!

III. Presentations on area of arch + by PL, Thm.